



Bernard Riemann :: SLS 2.0 :: Paul Scherrer Institut

Lattice concept of and news on the SLS 2.0 upgrade

XXVI ESLS Workshop, 2018-11-27, Krakow, Poland

Outline

- why Longitudinal Gradient Bends (LGBs) need reverse bends (RBs) to properly reduce emittance

➤ BR & Andreas Streun: *Low emittance lattice design from first principles: reverse bending and longitudinal gradient bends* arXiv:1810.11286
(submitted to PRAB)

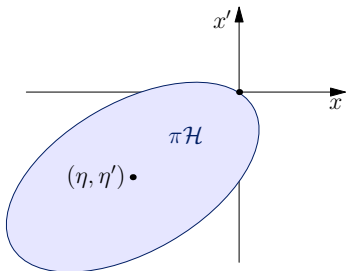
- SLS 2.0 lattice
- trajectories through combined-function magnets
- emittance coupling

Radiation integrals

➤ R.H. Helm et al., Proc. PAC 1973, p. 900

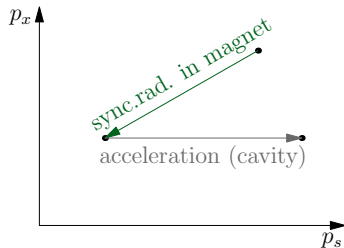
Equilibrium emittance $\varepsilon \propto I_5/I_2$

Quantum excitation (I_5)



- oscillation around dispersive orbit after energy loss
- loss probability depends on orbit curvature $b(s)$.
- minimize $I_5 = \int |b^3(s)| \mathcal{H}(s) ds$

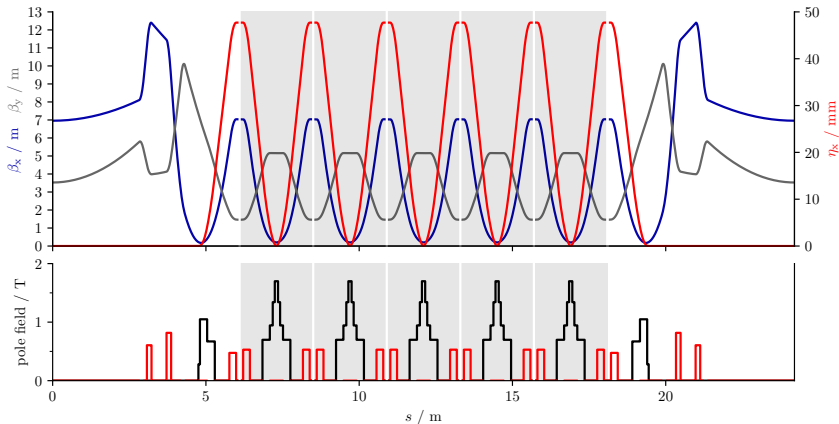
Radiation damping (I_2)



- damping of transverse momenta
- longitudinal acceleration
- maximize $I_2 = \int b^2(s) ds$

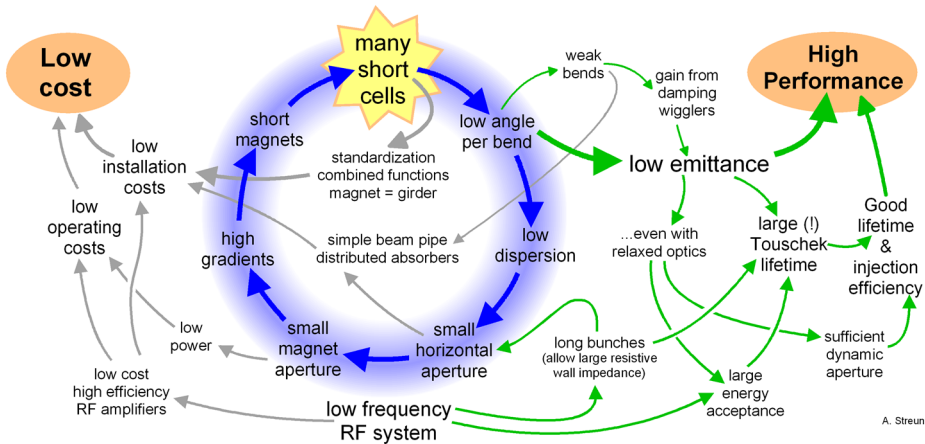
Multi-bend achromat (MBA)

historical review: ➔ D. Einfeld, Synchrotron Radiation News 27(6), p.4 (2014).



- M bending magnets, $M - 2$ **unit cells** with angle $2\theta_0$,
2 matching cells with one bend (θ_0) each. \rightarrow MBA angle $2(M - 1)\theta_0$
- emittance $\varepsilon \propto \theta_0^3 \propto (M - 1)^{-3}$, increase M within technical limits.

MBA optimization cycle

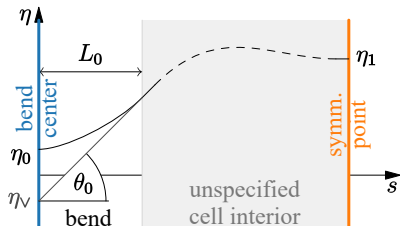


For large M , unit cells dominate the emittance.

Unit cell

Figures of merit

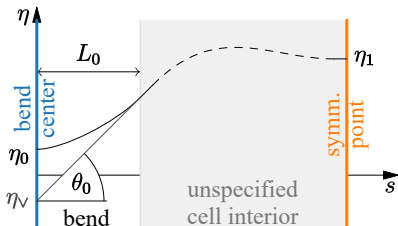
- Emittance for given bending angle
- Cell length, chromaticity
 \Rightarrow low phase advance 2ϕ per cell
- moderate focusing (lower limits on β_0 in bend center)
- plot emittance as a function $\varepsilon(\beta_0, \phi)$.



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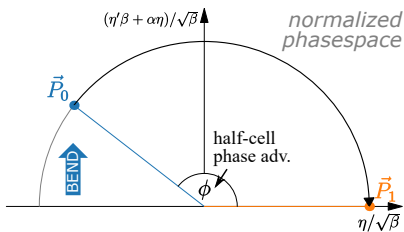


Half-cell model

- bend center: symmetry point of $\beta(s), \eta(s)$.
- For matching, model behaviour of $\eta(s)$ outside bend via η_V .

Unit cell

Half-cell model (continued)



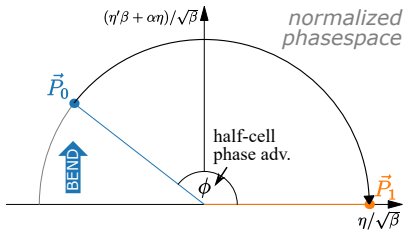
- Matching condition yields

$$\eta_0 = \underbrace{\eta_v(\beta_0, \phi)}_{\text{cell optics}} + \underbrace{\int_0^{L_0} s \cdot b(s) ds}_{\text{magnet-specific}}.$$

- β_0, ϕ and magnet profile $b(s)$ fully define emittance.

Unit cell

Half-cell model (continued)

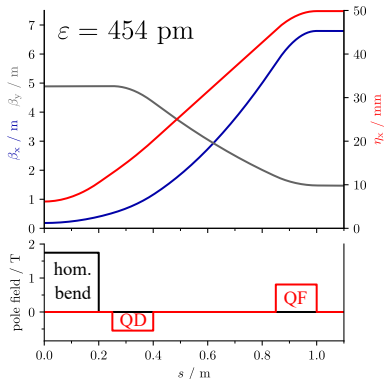


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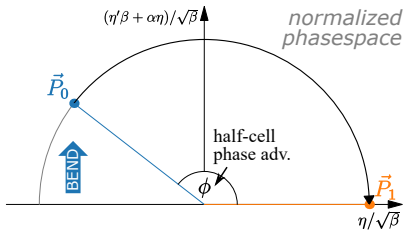
A typical example cell (at 2.4 GeV)



- emittance is ≈ 3.5 -times larger than the theoretical minimum emittance ($\varepsilon_{\text{TME}} = 121 \text{ pm}$).

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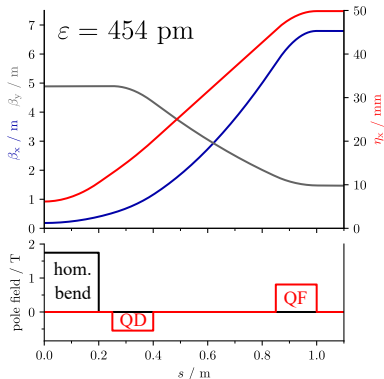


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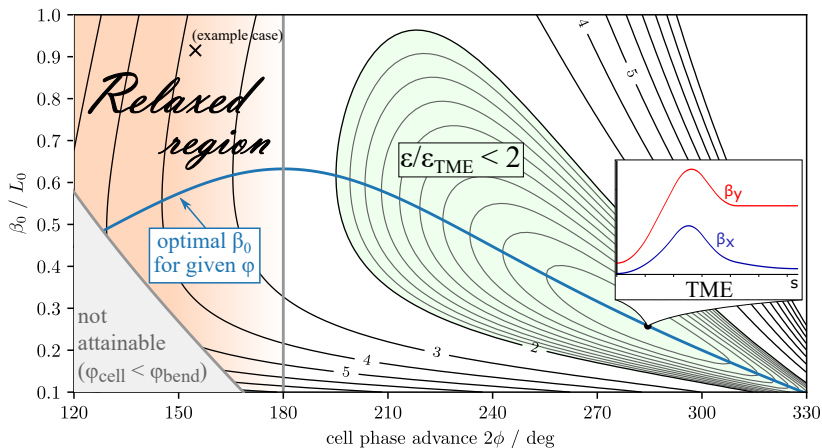


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☹ Why?

(relaxed) TME cell

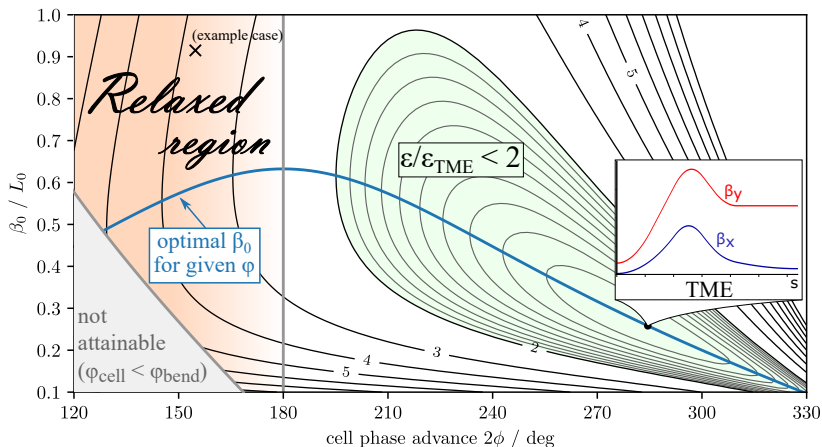
➡ L. C. Teng, Tech. Rep. ANL LS-17 (1987).



➡ Relaxed optics parameters and low-emittance region not overlapping.

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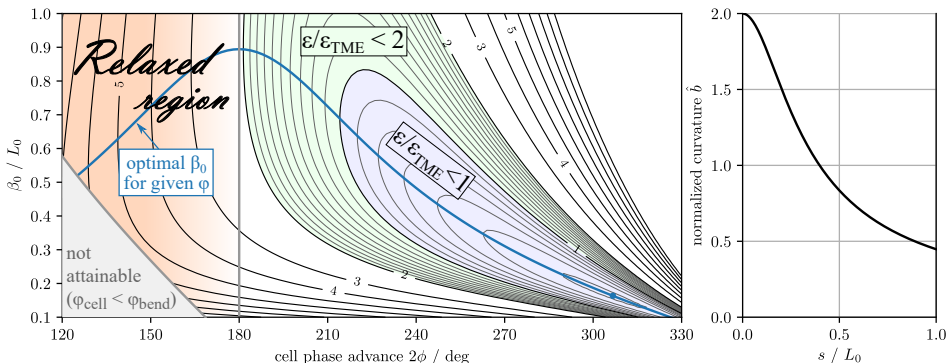
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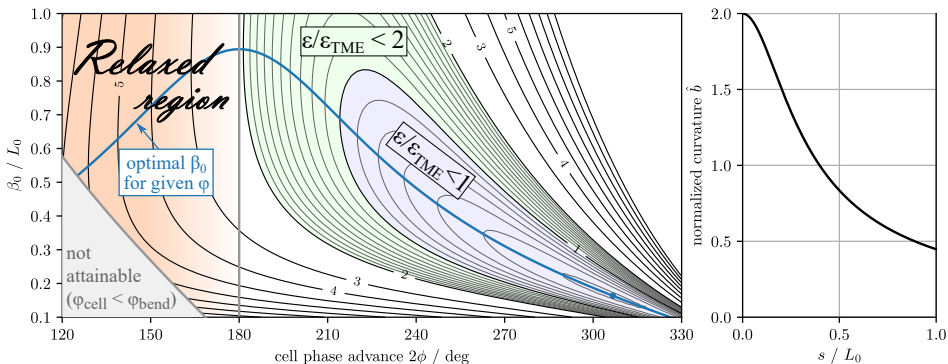
? What happens if magnet profile $b(s)$ is not constant?

cell with example LGB



- concentrated field in magnet center.
- low emittance at large phase advances, but cannot be used
- ☹ $\epsilon > 2\epsilon_{\text{TME}}$ **in relaxed region.**

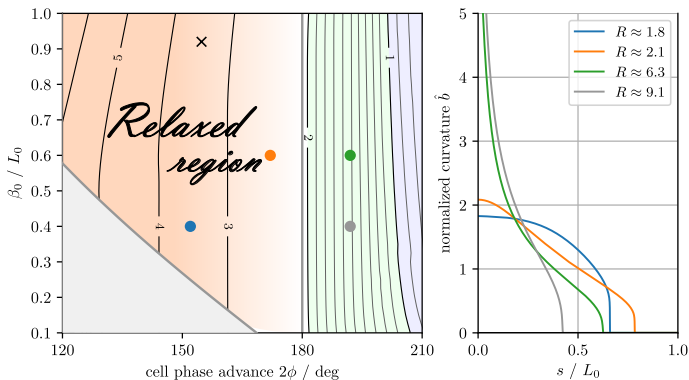
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- ? What happens if magnet profile $b(s)$ is optimized for each β_0, ϕ ?

Free-form LGB cell

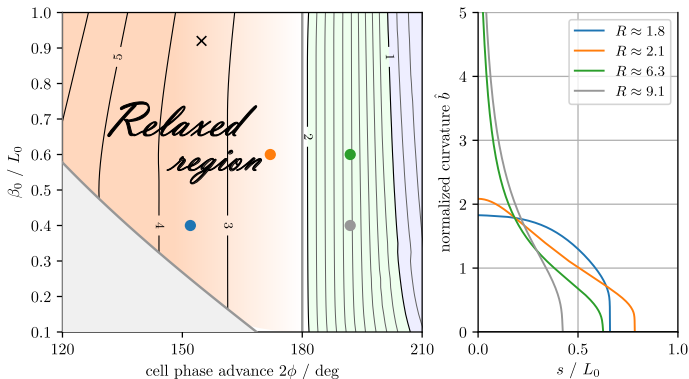
positive curvature, $b(s) \geq 0$



☹ a principle performance limit seems to exist: $\varepsilon > 2\varepsilon_{\text{TME}}$ for $2\phi < 180^\circ$.

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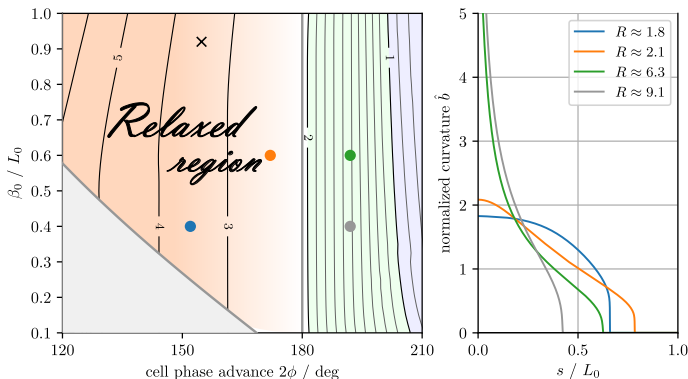


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- qualitative explanation: lower bound on $\eta_0 > \eta_V > 0$

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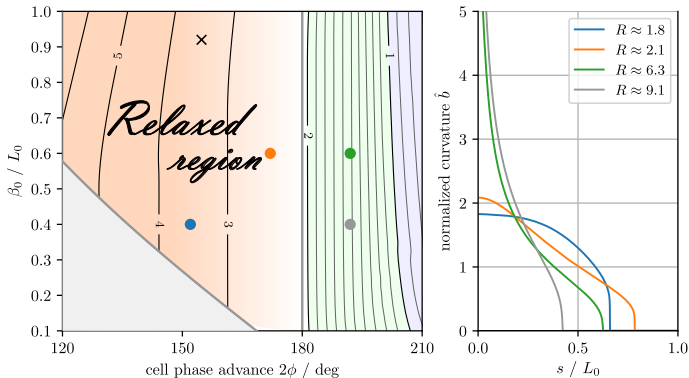


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👉 LGBs with positive curvature have only marginal benefits to homogeneous bends (when using only one type of bend..)

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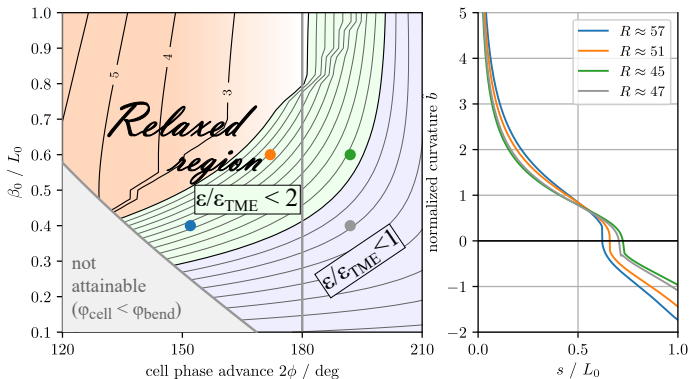
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? many $b(s)$ shapes fall off to zero - what happens if the constraint $b(s) \geq 0$ is removed?

Free-form LGB cell

arbitrary curvature



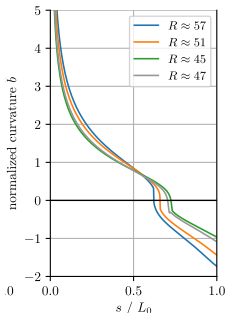
- Constraint on polarity of magnetic field is lifted, $b(s) < 0$ is possible.

☺ *significant emittance reduction* $\epsilon < 2\epsilon_{TME}$ occurs with $2\phi < 180^\circ$!

- 👉 near the end of the bending magnet, the polarity of the magnetic field is *reversed*.

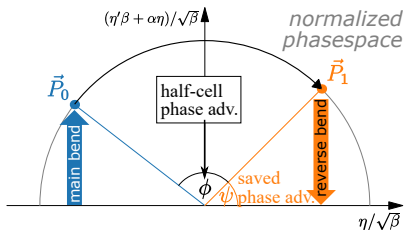
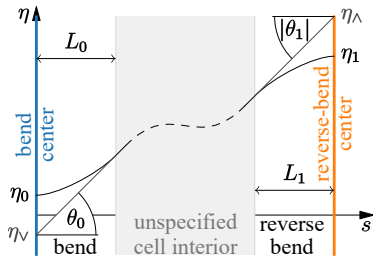
(thin-lens) reverse-bend cell

➔ A. Streun, Nucl. Instrum. Methods Res. A 737, p. 148 (2014)



- Bend can interpreted as a combination of
 - main bend near magnet center
 - reverse bend near magnet end
 - In this setup, focusing is applied at the end of the half-cell.
- ➔ Very similar to unit cell of above reference!
- 👉 Study a general setup, similar to (relaxed) TME cells.

A unit cell with two bends

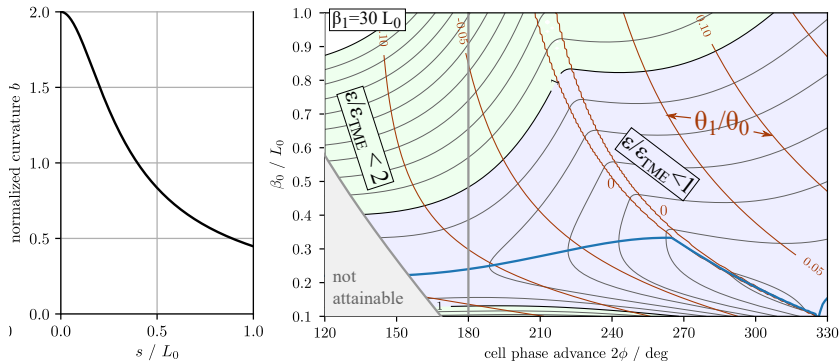


Half-cell model

- insert a homogeneous bend with half-kick angle $\theta_1 < 0$ at the half-cell end.
- phase advance relative to the one-bend case is *reduced*:

$$\phi = \phi_{\text{oneBend}} - \psi.$$
- large β at the reverse bend end helps.

LGB/RB cell with moderate LGB shape



- Here, length of homogeneous reverse bend $L_1 \sim |\theta_1/\theta_0| L_0$.
- ☺ $\epsilon < 2\epsilon_{\text{TME}}$ for relaxed region.
- ☺ Field enhancement OK (LGB not too strong).
- ☺ weak and small reverse bend.

Preliminary Conclusion

With reasonable focusing in unit cells

(cell phase advance $2\phi < 180^\circ \rightarrow$ short cells, low chromaticity)...

- common relaxed TME cells not suited very well for low emittances.

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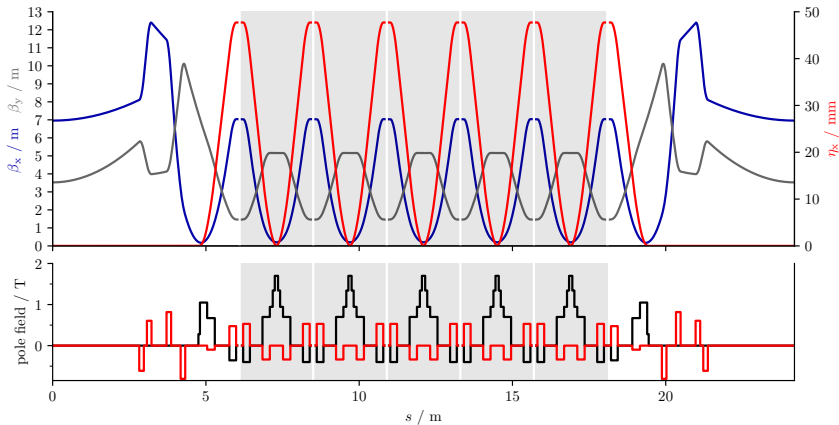
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- ☺ LGB-RB cells yield very low emittances in the unit-cell model.
- ? Used only I_2, I_5 – what about the other radiation integrals?
 - I_1 momentum compaction: this integral is small ~~no~~ need for trading ε vs α , choose $\alpha < 0$ to suppress CBI (not shown here).
 - I_3 closely related to I_2 .
 - I_4 manipulation via combined dipole and quadrupole fields (horizontal damping partition J_x)

the 7BA for SLS 2.0

see also ➔ A. Streun, T. Garvey et al., J. Synchrotron Radiat. 25, 631 (2018)

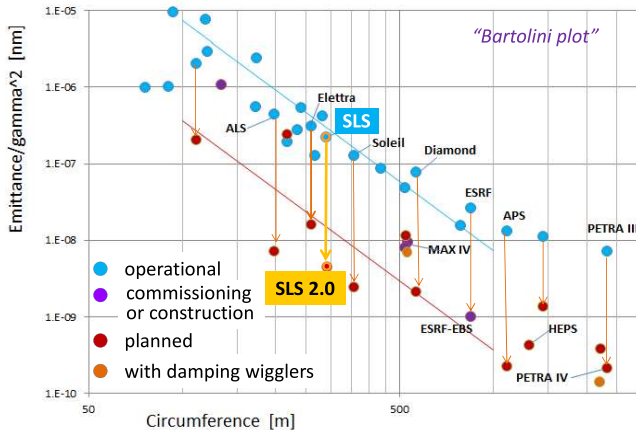


- LGB and RB merge with adjacent quadrupoles (combined-function lattice, damping partition $J_x \sim 1.7$).
- due to $\varepsilon \propto I_5 / (I_2 J_x)$, emittance is reduced to $99 \text{ pm} < \varepsilon_{\text{TME}}$.

the new generation of SL sources

Emittance normalized to energy vs. circumference

$$\epsilon_x \propto (\text{Energy})^2 / (\text{Circumference})^3$$



Theoretical
Emittance scaling
 $\epsilon \propto \gamma^2 C^{-3}$
 $\ln \frac{\epsilon}{\gamma^2} = K - 3 \cdot \ln C$
 $K \approx 2 \rightarrow \approx -1$
improvement $\times 20$

↑ upgrade
↓ projects

storage ring parameters

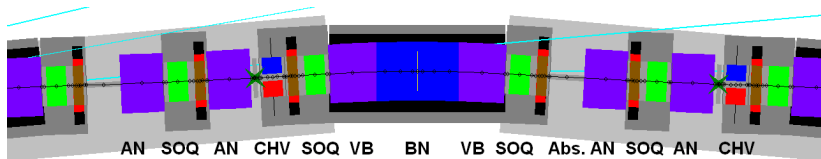
see also [↗ SLS-2 Conceptual Design Report \(2017\)](#)

energy	2.4 GeV
max. current	400 mA
rf system	500 MHz, 3HC
vert. emittance	10 pm

	SLS	SLS 2.0
circumference	288 m	290.4 m
buckets	480	484
periodicity	3	12
horiz. emittance @ 0 mA	5.5 nm	101 pm
@ 400 mA	5.5 nm	125 pm
rel. energy spread @ 0 mA	8.6×10^{-4}	1.04×10^{-3}
@ 400 mA	8.6×10^{-4}	1.08×10^{-3}
bunch length without 3HC	~ 40 ps	23 ps
– with 3HC	~ 100 ps	70 ps

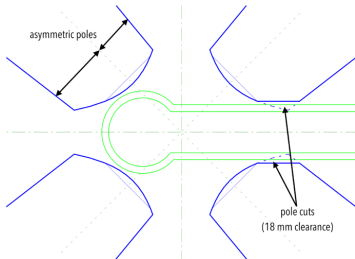
SLS 2.0 unit cell

➔ A. Streun, Tech. Report SLS2-SA81-004 (Sep. 2018)

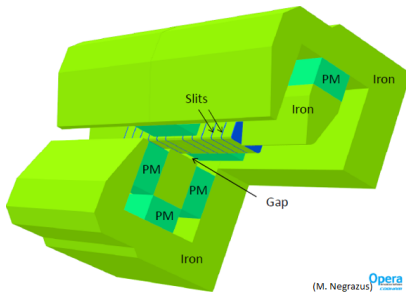


AN: hor. focusing reverse bend

BN/VB: vert. focusing LGB



- off-centered quadrupole yoke

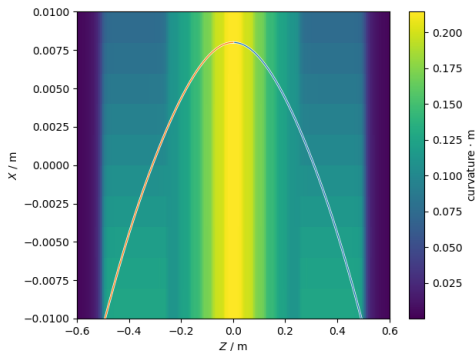


(M. Negruzis) 

- stacked permanent magnets in iron yoke.

BN/VB magnetic field

continuation of ➦ M. Aiba et al., Nucl. Instrum. Methods Res. A **892**, p. 41 (2018)



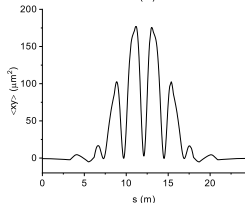
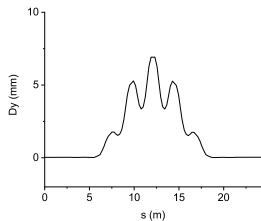
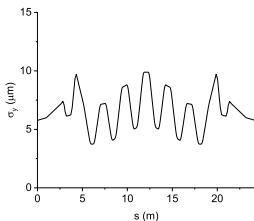
- build continuous field map from 'pixel input'
- compute closed-orbit trajectory by standard means (Runge-Kutta)
- compute focusing terms via derivatives of magnetic field and curvature

vertical emittance control using dispersion

M. Aiba, M. Böge

- Dispersion bump is excited with dispersive skew quads in the arc
- Coupling is excited at the same time but it is suppressed by non-dispersive skew quads in the straight section
- Possible setting:

	K1(m-2)
CSXX	-0.17983
CSXY	0.001074
CSYY	0.002835
CSYM	-0.19539
CSXM	-0.28117
CSY2	-0.24031
CSY2	-0.1748
CSX2	-0.19683
CSY2	-0.14275
CSY1	-0.13676
CSX1	-0.10322
CSY1	-0.1037
CSY1	-0.1037
CSX1	-0.10322
CSY1	-0.13676
CSY2	-0.14275
CSX2	-0.19683
CSY2	-0.1748
CSY2	-0.24031
CSXM	-0.28117
CSYM	-0.19539
CSYY	0.002835
CSXY	0.001074
CSXX	-0.1748



Dispersion and its derivative along the straight section are zero. Actually, the coupling in the arc is rather large, and thus the emittance is increased through dispersion+coupling

288 skew Qs

Thank you for your attention!

Acknowledgments

- A. Streun
- M. Aiba
- M. Böge

and many others

